

# Case Study of RC Slab Bridge using Nonlinear Analysis

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**Abstract -** After 2001 Gujarat Earthquake and 2005 Kashmir Earthquake, there is a nation-wide attention to the seismic vulnerability assessment of existing buildings. There are many literatures available on the seismic evaluation procedures of multi-storied buildings using nonlinear static (pushover) analysis. There are presently no comprehensive guidelines to assist the practicing structural engineer to evaluate existing bridges and suggest design and retrofit schemes. In order to address this problem, the aims of the present project was to carry out a seismic evaluation case study for an existing RC bridge using nonlinear static (pushover) analysis. In present study 4 Span RC Slab Bridge existed in SH-12 in Karnataka, was selected and by defining FEMA 356 Auto hinges conducted Nonlinear Static (Pushover) Analysis using ATC 40 Capacity Spectrum Method and software SAP2000 was used to analyse the Bridge. The evaluation results presented here shows that the selected bridge does not have the capacity to meet the desired performance level and it requires retrofitting.

**Index terms**—RC Bridge, FEMA 356, Nonlinear Static (Pushover) Analysis, SAP 2000, ATC 40.

## I. INTRODUCTION

India has had a number of the world's greatest earthquakes in the last century. The north-eastern region of the country as well as the entire Himalayan belt is susceptible to great earthquakes of magnitude more than 8.0. After 2001 Gujarat Earthquake and 2005 Kashmir Earthquake, there is a nation-wide attention to the seismic vulnerability assessment of existing buildings. The seismic building design code in India (IS 1893, Part-I) is also revised in 2002. The magnitudes of the design seismic forces have been considerably enhanced in general, and the seismic zonation of some regions has also been upgraded. There are many literatures available that presents step-by-step procedures to evaluate multi-storied buildings. This procedure follows nonlinear static (pushover) analysis. The attention for existing bridges is comparatively less. However, bridges are very important components of transportation network in any country. The bridge design codes, in India, have no seismic design provision at present. A large number of bridges are designed and constructed without considering seismic forces. Therefore, it is very important to evaluate the capacity of existing bridges against seismic force demand. There are presently no

Comprehensive guidelines to assist the practicing structural engineer to evaluate existing bridges and suggest design and retrofit schemes. In order to address this problem, the present work carried out seismic evaluation for an existing RC bridge using Nonlinear static (pushover) analysis as per ATC 40 is used to verify the result.

## II. BRIDGE LOADING

### A. Dead Load

It is a gravity loading due to the structure simply calculated as the product of volume and material density of the bridge.

### B. Live Loads

Road bridge decks have to be designed to withstand the live loads specified by Indian Roads Congress (I.R.C: 6-2010 Section II) [8]. In India, highway bridges are designed in accordance with IRC bridge code. IRC: 6 - 2010 – Section II gives the specifications for the various loads and stresses to be considered in bridge design. There are three types of standard loadings for which the bridges are designed namely, IRC class AA loading, IRC class A loading and IRC class B loading.

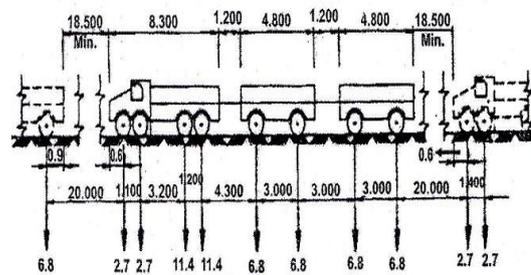


Fig 1. IRC Class a Loading

Class A loading<sup>[9]</sup> consists of a wheel load train composed of a driving vehicle and two trailers of specified axle spacing (Fig 1). This loading is normally adopted on all roads on which permanent bridges are constructed.

### C. Impact Load

For I.R.C. class A loading. The impact allowance is expressed as a fraction of the applied live load and is computed by the expression,

$I=4.5/(6+L)$

Where,  $I$ =impact factor fraction,  $L$ = span in meters.

#### D. Seismic Load

If a bridge is situated in an earthquake prone region, the earthquake or seismic forces are given due consideration in the analysis<sup>[10]</sup>. An earthquake causes vertical and horizontal forces in the structure that will be proportional to the weight of the structure. IS: 1893 Part-3 is referred for the actual design loads.

### III. NONLINEAR STATIC (PUSHOVER) ANALYSIS

The use of the nonlinear static analysis came in to practice in 1970's but the potential of the pushover analysis has been recognized for last 10-15 years<sup>[1]</sup>. This procedure is mainly used to estimate the strength and drift capacity of existing structure and the seismic demand for this structure subjected to selected earthquake. This procedure can be used for checking the adequacy of new structural design as well. Pushover analysis<sup>[2]</sup> is defined as an analysis wherein a mathematical model directly incorporating the nonlinear load-deformation characteristics of individual components and elements of the structure shall be subjected to monotonically increasing lateral loads representing inertia forces in an earthquake until a 'target displacement' is exceeded. Target displacement is the maximum displacement (elastic plus inelastic) of the structure at top expected under selected earthquake ground motion. Pushover analysis assesses the structural performance by estimating the force and deformation capacity and seismic demand using a nonlinear static analysis algorithm. The seismic demand parameters are global displacements (at roof or any other reference point), storey drifts, storey forces, and component deformation and component forces. The analysis accounts for geometrical nonlinearity, material inelasticity and the redistribution of internal forces. Response characteristics that can be obtained from the pushover analysis are summarized as follows:

- a) Estimates of force and displacement capacities of the structure. Sequence of the member yielding and the progress of the overall capacity curve.
- b) Estimates of force (axial, shear and moment) demands on potentially brittle elements and deformation demands on ductile elements.
- c) Estimates of global displacement demand, corresponding inter-storey drifts and damages on structural and non-structural elements expected under the earthquake ground motion considered.
- d) Sequences of the failure of elements and the consequent effect on the overall structural stability.
- e) Identification of the critical regions, where the inelastic deformations are expected to be high and identification of strength irregularities (in plan or in elevation) of the building.

### IV. PUSHOVER ANALYSIS PROCEDURE

Pushover analysis is a static nonlinear procedure<sup>[5]</sup> in which the magnitude of the lateral load is increased monotonically maintaining a predefined distribution pattern along the height of the Structure. Structure is displaced till the 'control node' reaches 'target displacement' or structure collapses. The sequence of cracking, plastic hinging and failure of the structural components throughout the procedure is observed. The relation between base shear and control node displacement is plotted for all the pushover analysis. Generation of base shear – control node displacement curve is single most important part of pushover analysis. This curve is conventionally called as pushover curve or capacity curve. The capacity curve is the basis of 'target displacement' estimation. The seismic demands for the selected earthquake are calculated at the target displacement level. The seismic demand is then compared with the corresponding structural capacity or predefined performance limit state to know what performance the structure will exhibit<sup>[4]</sup>.

### V. NEED FOR NON-LINEAR STATIC (PUSHOVER) ANALYSIS

Conventionally, seismic assessment and design has relied on linear or equivalent linear (with reduced stiffness) analysis of structural systems. In this approach, simple models are used for various elements of the structure, which are subjected to seismic forces evaluated from elastic or design spectra, and reduced by force reduction (or behavior) factors. This ensures displacements are amplified to account for the reduction of applied forces. The reduced force-amplified deformation linear elastic approach fails to fit within the principle of failure mode control, which is part of performance based assessment and design. This in turn has led to an increase in the use of inelastic analysis as a more realistic means of assessing deformational state in structures subjected to strong ground motions. The pushover analysis is a significant step forward by giving consideration to those inelastic response characteristics that will distinguish between good and bad performance in severe earthquakes. The nonlinear static pushover analysis is a partial and relatively simple immediate solution to the complex problem for predicting forces and deformation demands imposed on the structure and its elements due to ground motions. The pushover is part of an evaluation process and provides estimates of demands imposed on structures and elements. Hence, there is always a need of a method which is rational and accurate and at the same time able to identify seismic deficiencies correctly and that too in a correct order of vulnerability. Pushover analysis is able to satisfy these criteria satisfactorily and in a convenient way.

### VI. CAPACITY SPECTRUM METHOD (ATC 40)

In this method the maximum inelastic deformation of a nonlinear SDOF system can be approximated from the

maximum deformation of a linear elastic SDOF system with an equivalent period and damping. This procedure uses the estimates of ductility to calculate effective period and damping. This procedure uses the pushover curve in an acceleration-displacement response spectrum (ADRS) format. This can be obtained through simple conversion using the dynamic properties of the system. The pushover curve in an ADRS format is termed a ‘capacity spectrum’ for the structure. The seismic ground motion is represented by a response spectrum in the same ADRS format and it is termed as demand spectrum (Fig. 2).

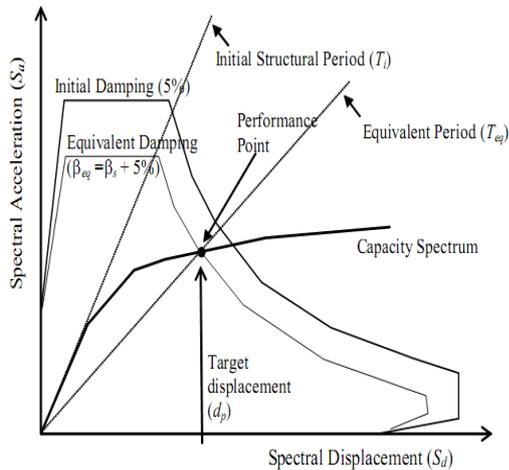


Fig 2. Schematic representation of Capacity Spectrum Method (ATC 40)

The equivalent period ( $T_{eq}$ ) is computed from the initial period of vibration ( $T_i$ ) of the nonlinear system and displacement ductility ratio ( $\mu$ ). Similarly, the equivalent damping ratio ( $\beta_{eq}$ ) is computed from initial damping ratio and the displacement ductility ratio ( $\mu$ ). ATC 40 provides the following equations to calculate equivalent time period ( $T_{eq}$ ) and equivalent damping ( $\beta_{eq}$ ).

### VII. PROBLEM DEFINITION

This chapter presents a summary of various parameters defining the computational models, the basic assumptions and the bridge geometry considered for this study. A 4 Span RC Slab Bridge existed at a chainage 12+334 in State Highway (SH-12) from Bijapur-Athani Section across Done River is taken as a case study. The bridge details are in Table 1 and Cross section of Bridge shown in Fig 3. The loads and load combinations on the bridge are studied and the same bridge is modeled in SAP 2000 (Fig 4), data and factors used for analysis are shown in Table 2. and after that conducted Linear static, Modal and Seismic Analysis (Response Spectrum) to get the maximum bending moments and dynamic properties of the bridge. Afterwards the FEMA 356 Hinges are defined in the model and conducted Nonlinear Static (Pushover) Analysis using ATC-40 to calculate Base Shear vs. Displacements, Effective time, Spectral Displacement Capacity & Spectral Displacement Demand and to find out Performance points of Bridge.

Bridge Details		
SLNo	Description	
1	Span of Bridge	20m X 4
2	Width of Bridge	8.6 m
3	Lanes	2 Lanes
4	Number of Main Girders	3 No's
5	Total depth	2.495 m
6	Slab thickness (average)	0.26m
7	Type of Loading	IRC class A Train
8	Loads	DL+LL+IL+EQ
9	Compressive Strength of Concrete (fck) (MBO)	30000 KN/m <sup>2</sup>
10	Modulus of Elasticity E=5000vfck E=5000v30 = 30000 N/mm <sup>2</sup>	27386128 KN/m <sup>2</sup>
11	Poisson's Ratio of Concrete	0.18
12	Type of Analysis	Linear & Nonlinear

Table 1. Bridge Details

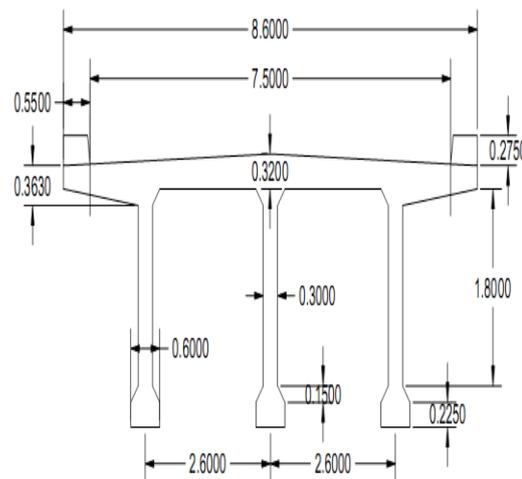


Fig 3. Cross Section of Bridge

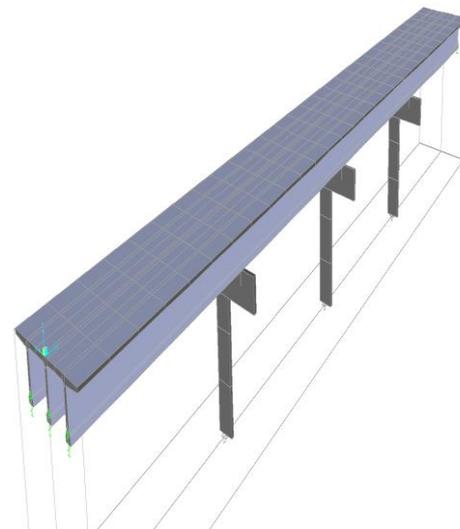


Fig 4. Bridge Model in SAP 2000

Input Data for Analysis		
Sl.No	Particulars	
1)	Density of Reinforced Concrete	25000 KN/m <sup>3</sup>
2)	Grade of Concrete	M-30
3)	Type of live load	IRC Class A Train
4)	Impact Factor (i) $\frac{4.5}{6 + L}$	0.173
5)	Importance Factor (I)	1.2
6)	Response Reduction Factor (R)	3.0
7)	Poisson's Ratio of Concrete	0.18
8)	Seismic Zone	Zone III
9)	Seismic Zone Factor	0.16
10)	Soil Type	Type II

Table 2. Input Data in SAP 2000

**A) Modeling of Flexural hinges**

In the implementation of pushover analysis, the model must account for the nonlinear behavior of the structural elements. In the present study the plastic hinge is assumed to be concentrated at a specific point in the frame member under consideration. In this study flexure (M3) hinges (FEMA 356 - Auto hinges) (Fig 5) modeled at possible plastic regions under lateral load. Properties of flexure hinges must simulate the actual response of reinforced concrete components subjected to lateral load.

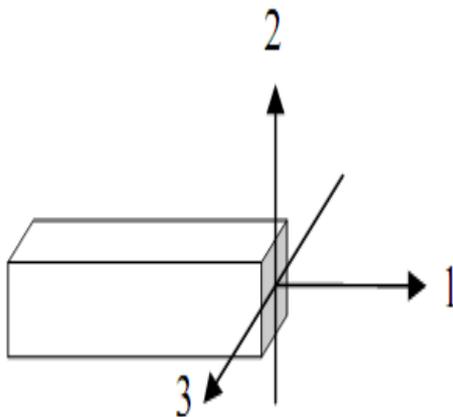


Fig 5. Coordinate system used to define the flexural hinges

Flexural hinges in this study are defined by moment-rotation curves calculated based on the cross-section and reinforcement details at the possible hinge locations. For calculating hinge properties it is required to carry out moment-curvature analysis of each element. Constitutive relations for concrete and reinforcing steel, plastic hinge length in structural element are required for this purpose.

**B) Moment-rotation parameters**

Moment-rotation parameters are the actual input for modeling the hinge properties and this can be calculated from the moment-curvature relation. The moment-rotation curve can be idealized as shown in Fig 6 and can be derived from the moment-curvature relation. The main points in the

moment-rotation curve shown in the figure can be defined as follows:

- 1) The point 'A' corresponds to the unloaded condition.
- 2) The point 'B' corresponds to the nominal yield strength and yield rotation  $\theta_y$
- 3) The point 'C' corresponds to the ultimate strength and ultimate rotation  $\theta_u$ , following which failure takes place.
- 4) The point 'D' corresponds to the residual strength, if any, in the member. It is usually limited to 20% of the yield strength, and ultimate rotation,  $\theta_u$  can be taken with that.
- 5) The point 'E' defines the maximum deformation capacity and is taken as  $15\theta_y$  or  $\theta_u$ , whichever is greater

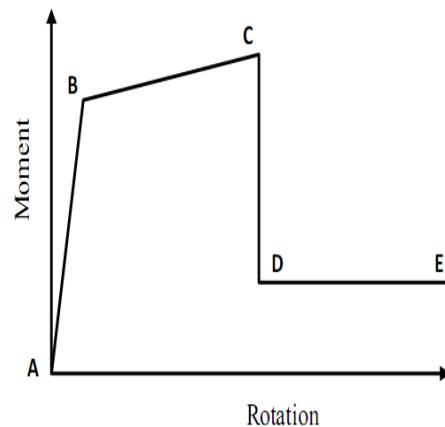


Fig 6. Idealized moment-rotation curve of RC elements

**VIII. RESULTS**

The selected bridge model is analyzed using Nonlinear Static (Pushover) analysis. This chapter presents Pushover analysis results. Pushover analysis (Push Y) was performed first in a load control manner to apply all gravity loads on to the structure (gravity push). Then a lateral pushover analysis in transverse direction (Y-direction) was performed in a displacement control manner starting at the end of gravity push. The results obtained from these analyses are checked by comparing spectral displacement demand and spectral displacement capacity from the pushover curve (Graph 2).

**A) Nonlinear static (pushover) analysis**

Nonlinear Static (Pushover) Analysis permits to identify critical members likely to reach limit states during the earthquake. Nonlinear Static Analysis is carried out after assigning flexural hinges (FEMA 356 Auto hinges) using ATC 40 Capacity Spectrum Method. As a result performance points & levels (IO, LS, and CP) are found in different pushover steps (Fig 8 to Fig 13) and Base shear vs. Displacement Graph (Graph 1) & Spectral Acceleration vs. Spectral Displacement Graph (Graph 2) is drawn and Spectral Displacement Demand & Spectral Displacement Capacity is calculated.

Flowchart<sup>[7]</sup> outlining a procedure using static push-over analysis in seismic design and retrofit evaluation is shown in fig 7.

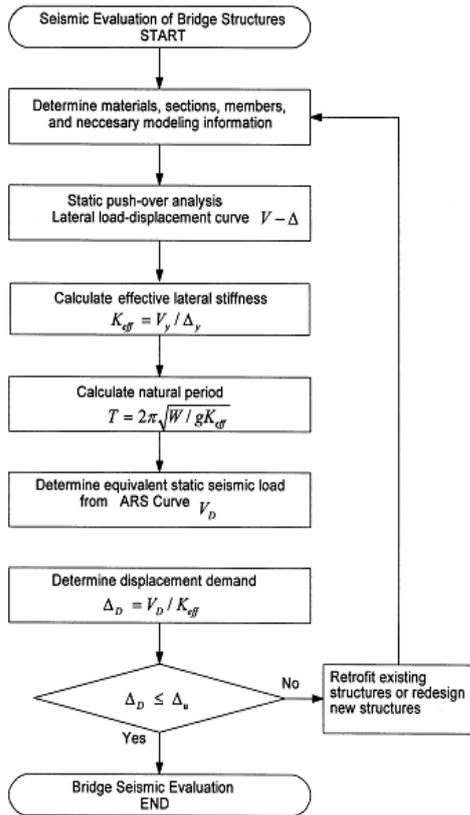
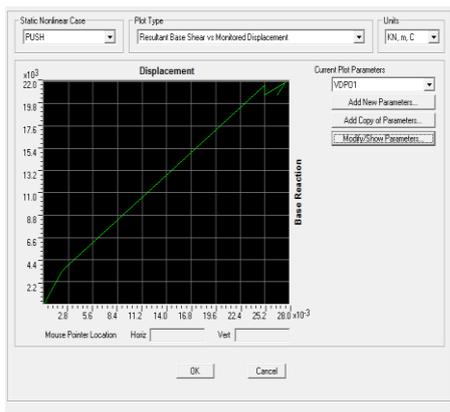


Fig 7. Flowchart of Static Pushover Analysis

Pushover Curve - PUSH		
Step	Base Shear KN	Displacement m
0	0	0
1	3105.297	0.00199
2	3606.609	0.002397
3	21609.991	0.02516
4	20626.293	0.02517
5	21960.929	0.027578
6	20547.83	0.02653

Table 3. Base Shear vs. Displacement

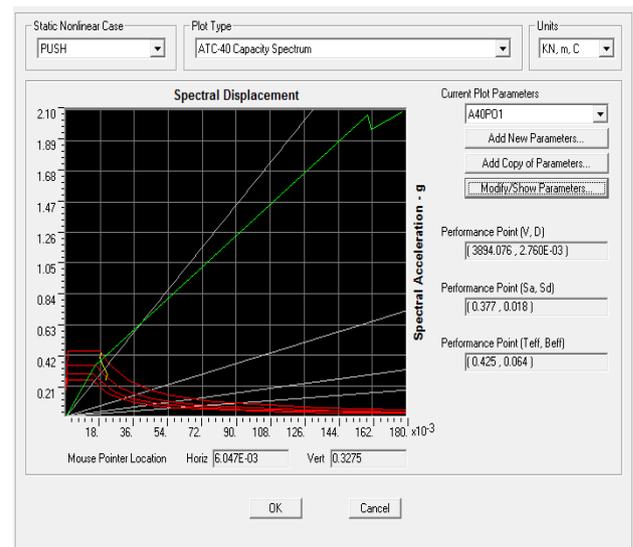


Graph 1. Base Shear vs. Displacement

Pushover Curve Demand Capacity - ATC40 - PUSH				
Step	T <sub>eff</sub>	B <sub>eff</sub>	Sd Capacity (m)	Sd Demand (m)
1	0.414959	0.05	0	0.018554
2	0.414959	0.05	0.012881	0.018554
3	0.422873	0.063618	0.015547	0.017778
4	0.557828	0.081033	0.15941	0.021952
5	0.574937	0.108421	0.161382	0.020765
6	0.585788	0.114581	0.178023	0.020797

Table 4. Pushover Demand Capacity Curve

(ATC 40)



Graph 2. Pushover Demand Capacity Curve

(ATC 40)

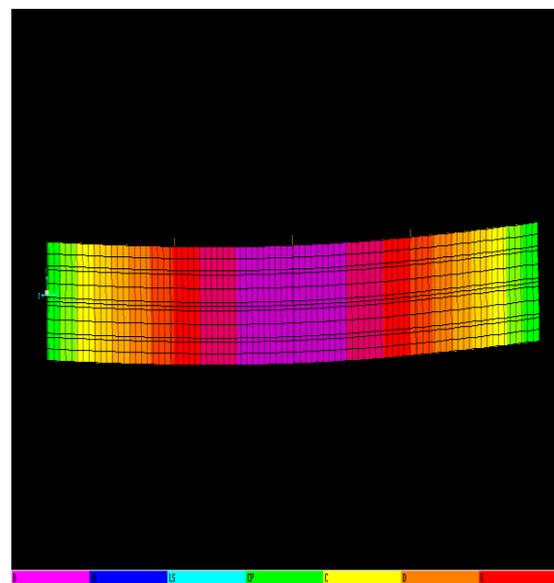


Fig 8. Pushover Step 1

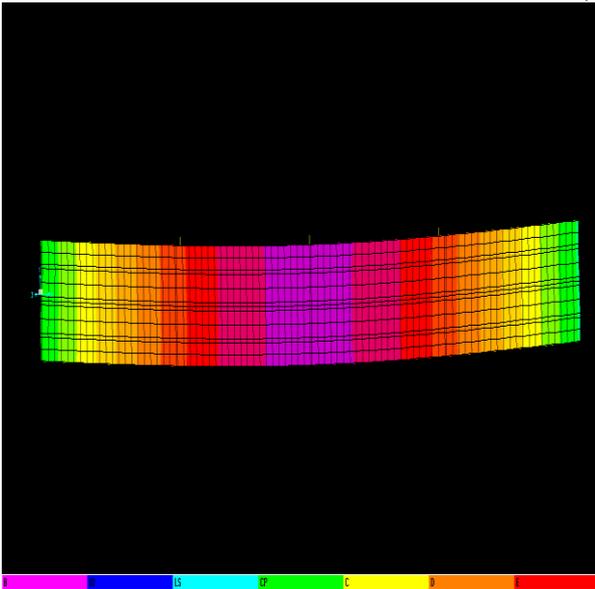


Fig 9. Pushover Step 2

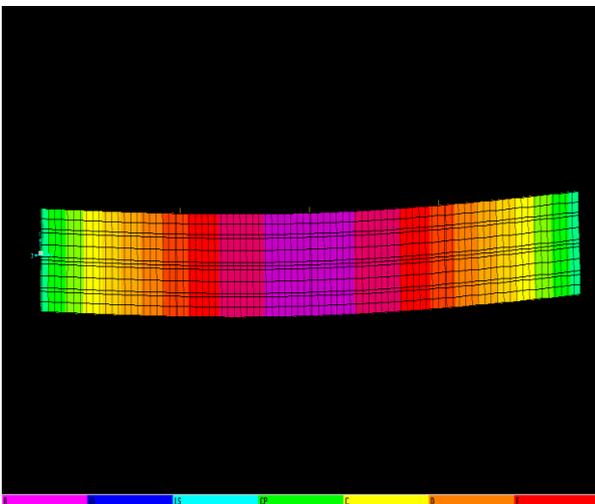


Fig 10. Pushover Step 3

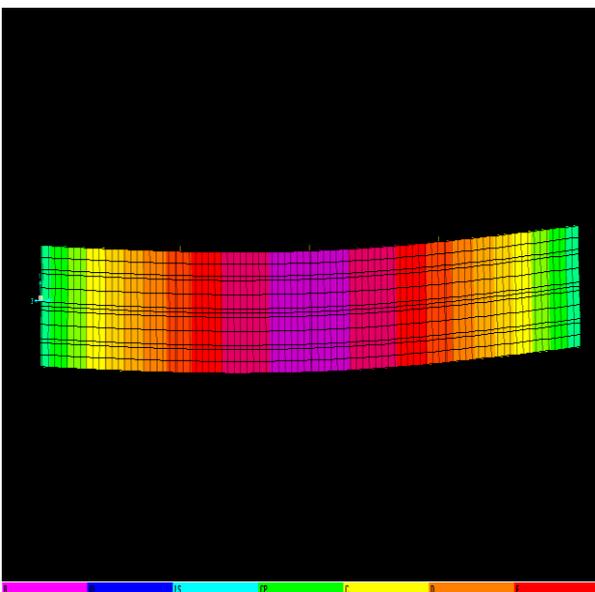


Fig 11. Pushover Step 4

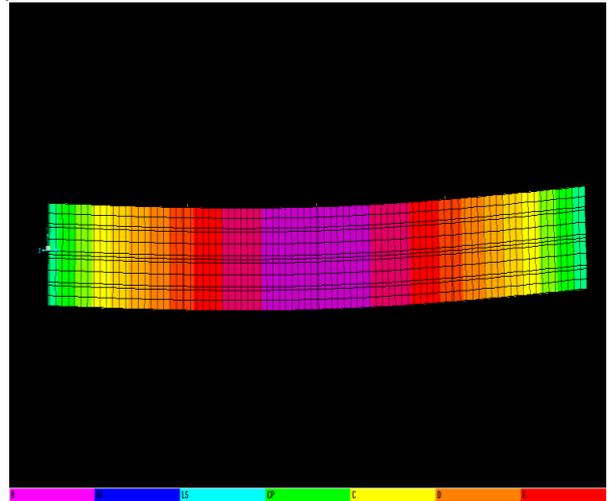


Fig 12. Pushover Step 5

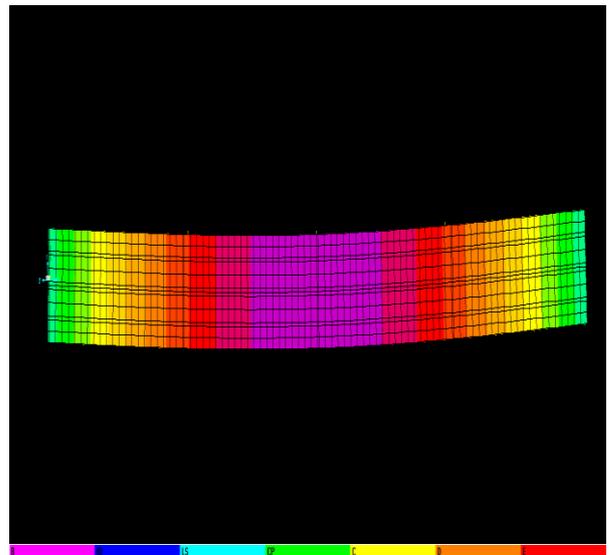
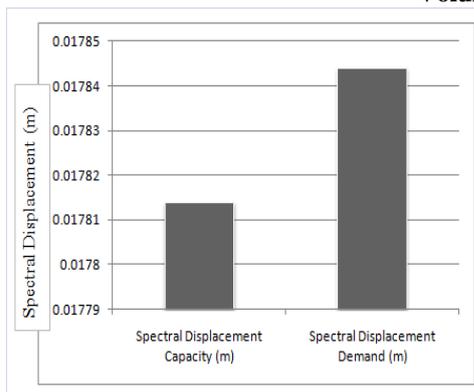


Fig 13. Pushover Step 6

The effective time is 0.425; it is in between pushover step 3 and step 4. At effective time the Spectral Displacement Capacity (m) and Spectral Displacement Demand (m) is calculated by interpolating values in the Table 4. The table 5 shows the Spectral Displacement Capacity and Spectral Displacement Demand values according to Capacity Spectrum Method ATC 40 at effective time 0.425 sec's and schematically it are represented in Graph 3.

Pushover Step	Effective Time, $T_{eff}$ (Sec)	Spectral Displacement Capacity (m)	Spectral Displacement Demand (m)
Between 3 & 4	0.425	0.017814	0.017844

Table 5. Comparison between Capacity & Demand (ATC 40)



Graph 3. Comparison between Sd Capacity & Sd Demand

### IX. CONCLUSION

Under Seismic Load, Base Shear v/s Displacement and By Pushover Analysis the performance levels of bridge are studied. From the Analysis it is evident that Spectral Displacement Demand is more than the Spectral Displacement Capacity in the analyzed Bridge. So the analyzed bridge requires retrofiting.

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### X. ACKNOWLEDGMENT

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