

# Error Performance Analysis of LMS and RLS Adaptive Filters Parametric Study

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**Abstract**—The adaptive filter design is the still essential field of research. Since the acquired modulated data is suffered from AWGN additive noise while transmitted. Thus with the sophisticated receivers hardware's it is essential to design the adaptive filters at the front end. Filtering is intended to eliminate the AWFN noise. Investigating adaptive filter algorithms viz Least Mean Square LMS, normalized LMS (NLMS), and Recursion based Least Square RLS algorithms is the goal of the paper. The sinusoidal signals are randomly generated with large sample size. The noisy and desired signal data are produced as delayed filter response. The performance is evaluated based on the measured mean square error using mentioned filter methods. The design parameters are varied for achieving optimum noise filtering. The NLMS method offers minimum error performance.

**Keywords**—Adaptive Filter, Neural Network, BPNN, ADALINE, Amplitude Modulation, AWGN Noise, Filter Design.

## I. INTRODUCTION

There are various cases in real-time signal processing systems when a desired and usable signal is destroyed by noise. Noise includes random noise, white noise with an uneven frequency distribution, and frequency-dependent noise. The term "noise" refers to any type of disturbance, whether induced by stimuli, the environment, or components of sensors and circuits, and does not only refer to thermal or flicker noise [1]. Noisy data can come from a variety of internal and external sources. This study's goal is to examine how adaptive filtering algorithms work and how well they function when used to cancel noise within an absence for an exemplary signal. The technique of extrapolating a desirable signal [2] based on noisy measurement is known as noise cancellations. If the qualities of the signal along with noise are not known. A flexible filter is required as circumstances changes the throughout time and performance [3]. The basic communication system representation along with the adaptive filter is shown in the Figure 1.

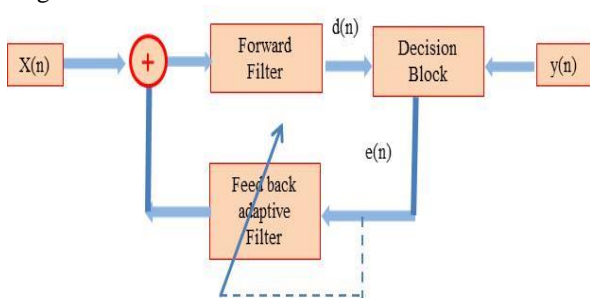


Fig. 1. An adaptive Filter Diagram Design

The basic adaptive filter system requires  $x(n)$  as the input sequences. And is passed to the forward FIR filter to generate the desired signals  $d(n)$  the actual predicted output sequences  $y(n)$  are produced using the decision block/ Then iteratively the weight of the filter are updated in feedback loop. To enable to discover the best filter, various adaptive filters approaches are being carried out and assessed in regards to noise cancellation accuracy. The LMS [1, 3, 4 and 14] and Normalized LMS [8, 12] including the RLS [5, 7 and 10] algorithms are required further studies. As indicated in Figure 1, an adaptive filter method requires a referred to as coefficient update across the feedback path. It is accomplished by using a weight update equation to compute new filter coefficients every each sample. The essence coefficient updating equation is as follows;

$$W^{n+1} = W^n + \text{del } W \quad (1)$$

Where  $W^{n+1}$  is new weight and  $\text{del } W$  s step size.

The efficient operation of the system is also evaluated by modifying the system's variables for adaption including filtering order, for performance improvement.. The various filter design parameters required for designing and MATLAB simulation are mentioned in the Table 1.

Table 1. Filter Design Parameters

Parameter	Description	Range
N	Number of Total Samples	10000
R	Average ensembles at 100 Ittr.	100
O	Order of filter function	12
S= del W	Step size LMS	0.02
B	Normalized Step NLMS	0.25
Delta	RLS coefficient scale	0.001
Lambda	Weight exponential factor	1
n0	sample delay	25
Wi	Initial weight	0.001

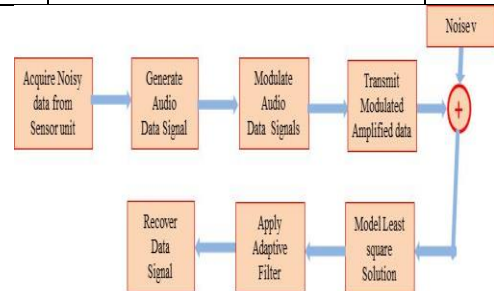


Fig.2.Basic communication system diagram using adaptive LMS filter

## II. COMMUNICATION SYSTEM WITH FILTER

The basic communication system block representation using the adaptive filter at front end is shown in Figure 2. It is evident that the filtering problem is initially modeled, and then weight adoption is done utilizing LMS-based assessment techniques. It can be observed that noise is essentially added to the actual signal at acquisition time and transmission time both. Thus filter is used at the front end of the receivers. The first step is the simulation of the amplitude modulated speech signal. The input signal of voice is mathematically represented by sinusoidal eq. as

$$d = \sin([1:N] * 0.05 * \pi) \quad (2)$$

The noisy Gaussian data  $v$  as shown in Figure 2 is randomly generated with the variance capacity of 0.25.

$$v1 = \text{fil}(v) @ [1, -0.8] \quad (3)$$

The desired input signal  $x$  is reproduced by accumulating noise and data as

$$x = d + v1 \quad (4)$$

Now the filtering problem is to find the optimal solution to eliminate the noise from the data.

## III. REVIEW OF RELATED WORK

Shubhra Dixit and colleagues [1] has presented a contemporary as well as historical study on adaptive filter approaches based on dynamical noise cancellation systems. Because signal characteristics in many noise suppression programs can vary rather quickly, adaptive algorithms which converge quickly are required. Fundamentals and most recent developments to boost resolution and minimize computational complexity for future implementation of techniques like LMS as well as RLS, which are critical in noise reduction, are reviewed. The goal of this work is to investigate numerous noise suppressing LMS algorithms and provide the reader with a synopsis of related research. Sudhanshu Ranjan-Dwivedi et al. [2] set out to create the delayed LMS (DLMS) as well as adaptive digital LMS (LMS) for typical noise removal applications. To minimize noise, a particular sound can be obtained with LMS algorithms in MATLAB.

They compare various ways on the framework of a sound wave provided by MATLAB running. Although high-speed transmission of sound is possible, the signal becomes loud when noise is introduced. We were unable to distinguish the initial sound from the background noise. The noise level associated with a noisy signal could be lowered using this method without affecting the signal's properties. Based on the data shown, the LMS algorithm outperforms the DLMS as well as TVLMS algorithms in actual work using MATLAB.

Amjad J. Huaidi and colleagues have presented an innovative modifications approach for FIR with IIR digital filters in framework of system identification. Fundamental LMS method is hybridized by using the GA (Genetic Algorithms) to develop the new unified learning process known as LMS-GA. Fundamental purpose of proposed learning tool was to avoid local minima, which

are a common problem in normal LMS algorithms and their variations, and to move closer to the global minimum by identifying optimum weights vector quantities when only projected data are given. When the typical LMS algorithm gets trapped in a local minimum, suggested LMS-GA technique uses GA to refresh the filter coefficients while exploring new regions in the search space

S. Saranraj et al [4].proposed that best suitable technique for changing the weights is to use Least Means Square (LMS) procedures. The LMS alters the weights through a small amount to reduce the likelihood of errors. LMS adaptive filtering for critical path attainment is presented to reduce adaption latency. Pipelines must be implemented in order to reduce adaptation latency. However, after it has passed the required sample period, the standard LMS adjustable filter is rendered unusable. A proportionate-type normalized LMS filter has been proposed in order to change the weights to an extent that lowers error and to create a low-cost equalizer for ASIC fulfillments.

B. K. Das with colleagues [5] presented the first as well as second order resolution assessment of the sparseness aware 10-RLS adaptable filter is reported in there paper. The average and mean square deviation for the adaptive filter parameter vector are given as steady state values as theorems. they have designed the duplex takeover. They stated that due to standard limited duplexer stop bands segregation, frequency division duplexing (FDD) transmitters receive a leakage (TxL) signal. Whenever paired with the receive mixer's second-order fluctuation, this TxL signal may trigger baseband (BB) second-order intermodulation distortion (IMD2) having a bandwidth that's double that of the transmit signal. Because of this nonlinear IMD2 interference, stream-to-interferences with-noise proportion of the desired receive signal may be drastically deteriorated in basic conversion receivers. This contribution proposes a nonlinear Wiener modeled recursive-least-squares (RLS) kind adaptive filter for cancelling IMD2 interference in digital BB. The channel-select and DC-notch filters included in the provided IMD2 replica also provide receiver front-end filtering.

In the [7] research have researched to present a discussion on several memory less as well as memory structures from a bilinear perspective. Using the Kronecker product decomposition concept, we design the multi linear RLS method after memory structures. In an echo cancellation setting, a number of models covering both long-length responses to impulses and the reverberating effect were conducted.

Weizhi Wang and colleagues [6] have proposed to design a limited partial update based NLMS method recommended in wireless communication systems since it overcomes the slow speed of converging of the LMS algorithm with the high computing complexities involved in the NLMS algorithm. This approach just modifies a subset of the filter's coefficients

during each modification, rather than all of them. Complexity of traditional dynamic filter algorithms has been significantly decreased. In this work, NLMS algorithm receives only a partial update, and its superiority is proved by comparing it with both the LMS methodology and NLMS technique using simulator validation.

Danilo Comminiello et al [7] have primarily proposed a technique which was linear in the parameters (LIP) linear filters that leverage functional link expansions. To improve the effectiveness of this type of functional link adaptive filters (FLAFs), we propose low-complexity expansions as well as frequency-domain adaptation of the values of the parameter. They additionally describe the partitioned-block frequency-domain FLAF, a component of this family of algorithms that is especially well suited to online nonlinear modeling problems. Danilo contrast two different frequency-domain FLAFs that use different expansions to find the best performance-to-computability trade-off.

The research outcomes had showed that, even under the adverse dynamic situations and even with limited processing resources, the given algorithms can be regarded as a cost-effective and efficient solution to earn online applications such as the Deepanjali Jain [8] has adapted suppression of noise research throughout the past and present using adaptable filter algorithms are reviewed in this work. Parametric noise cancellation, a large topic of communication investigation, is used to reduce speech signal noise. Because received signals vary rapidly in many applications, it is critical to use adaptable algorithms which converge quickly. The adaptive (LMS) algorithms employed in there paper for eliminating noise in voice signals provide effective performance at a relatively inexpensive computing cost. ‘

Pankaj Vyas et al. [9] defined a designing technique for adaptive filter foe modulated signals. Architectures of the NN based network model employed ADALINE and BPNN based neural network algorithms. They have specified the estimate error and mean square error effectiveness as well as declared that BPNN is the best

Q. Noman et al. [10] have widely used dynamically filtering techniques for tackling a wide range of challenges in digital communication systems. The parameters of the ANC-NLMS algorithm include the filter length ( $L_j$ ) parameter, which is calculated in a  $2n$  number sequence of 2, 4, 8, 16,... 2048, with the step size ( $n$ ), which is chosen at random using variable  $n$  (VSS) optimization. The approach is initially put through a series of experiments to discover the optimal  $n$  range of 11  $L_j$  values for the specific situation. Adaptive strategies based on the mathematical concept and processing difficulty for the mean-square-error cost functioning, such as (LMS) and therefore normalized version (NLMS), have been the most widely employed in communication system so far.

J. Chhikara and colleagues [11] had constructed an FPGA routing mechanism on the shared memory of a

multi-processor employing the Galois API, an application feature that allows possible parallels. The router employs path finder, which is the cornerstone of the vast majority commercial industrial FPGA routers. To decrease the amount to reversion that might occur as a result of erroneous theory, we route nets sequentially whilst overlapping an extension phase for each net. Jia-Haw Lee et al [12] have presented the good study of basic noise cancellation mechanism, depending on Minimum Mean Square offering (LMS) technique, is explored and improved with an updated filter. To simulate noise reduction, the LMS dynamic filter approach is utilized. The LMS adaptive filtering methodology takes two inputs: the engine's noise signal and a noise-tainted speech signal. The filtering of signal can be compared with the initial noise-free voice signal to emphasize the extent of attenuation in the noise message.

Hamidia M et al [13] used ultrasonic echo cancellation systems based on adaptive screening; we offer an enhanced variable step-size normalized least mean square (VSS-NLMS) algorithm in this study. For a non-stationary input, the stable-state error of the NLMS method with a fixed step-size (FSS-NLMS) is very high. This mistake can be minimized by using algorithms with dynamic step-size (VSS). G. Sunil Kumar et al [16] in there study discusses recent and previous studies on dynamic noise cancellation system-based adaptive filter techniques. The use of adaptive techniques that resolve quickly is necessary since the signal properties in many noise cancelling systems could change very quickly. Over all it is still required to compare the effectiveness of linear and recursive filtering for adoption quality.

#### IV. PROPOSED METHODOLOGY

The current paper describes a LMS based signal improvement and filtering system based on adaptive noise cancellation. In a communication system, sinusoidal voice signals are transmitted across a channel. the paper proposed to evaluate the noise cancelation problem using three filters as LMS, RLS and NLMS. The  $d(n)$  and the noisy signals are generated using the Eq (2), (3) and (4). Then systematic methodology is used for modeling the variable step and weight updating method for all three filters.

#### V. RESULTS AND EVALUATIONS

Examples of our adaptive filtering findings for sinusoidal voice signal modeling and filtering are shown in this section. The initial sinusoidal voice data is used for generating the desired and noisy data using the FIR filter as shown in eq (3) desired input and the AWGN noisy data are shown in the Figure 3. Figure has demonstrated the observation based on the noise at variance of 0.2

The reference signal is generated as the delayed version of input data at a window of 25 sample delay as shown in the Figure 4.

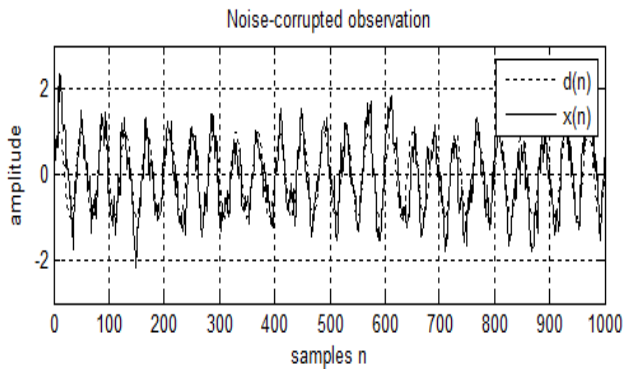


Fig.3.Simulation of the true data and noisy data

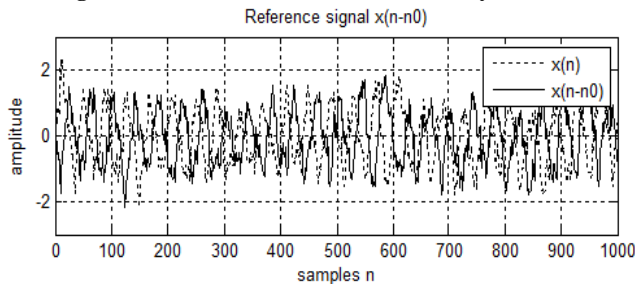


Fig.4.Simulation of the data using delay

The results comparison of the LMS, NLMS and RLS filters are given in the Figure 5 below.

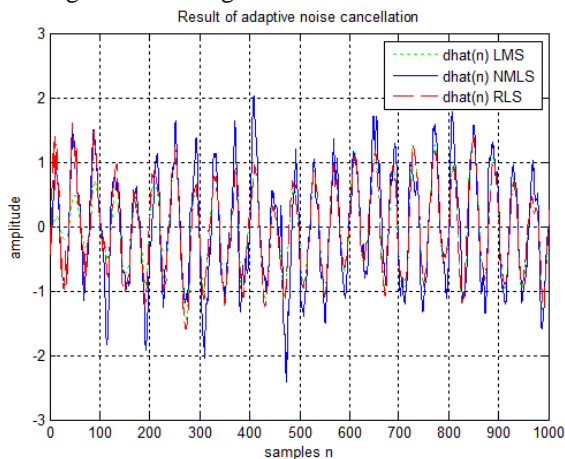


Fig. 5 Results comparison of qualitative assessment of the various filters filtering outcomes.

As it is difficult to assess the performance of filtering qualitatively therefore in this paper the performance is evaluated based on the MSE error calculated for three filtered data.

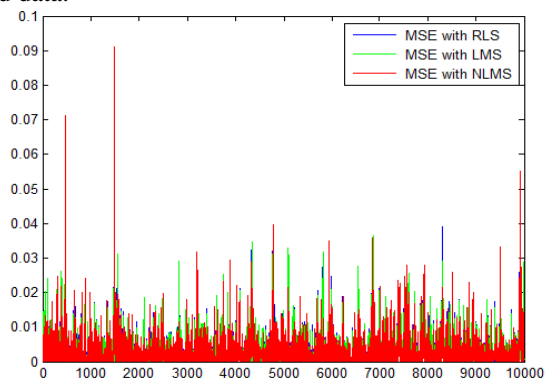


Fig.6. comparison of the mean square error valuated for RLS, LMS, and NLMS method.

It is observed that the NLMX method offers the minimum MSE performance and out performs among all.

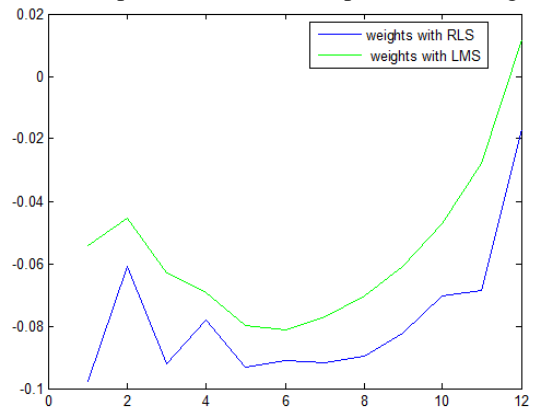


Fig.7 weights comparison for RLS and LMS approach.

## VI. CONCLUSIONS AND FUTURE WORK

The purpose of the study is to investigate adaptive filter techniques such as Least Mean Square LMS, normalized LMS (NLMS), and Recursion based Least Square RLS algorithms. The sinusoidal waveforms are generated at random with a large sample size. As a delayed filter response, the noisy and desirable signal data are created. The performance is evaluated using the given filter methods based on the measured mean square error. The design parameters are changed to get the best noise filtering. The NLMS approach has a low error performance.

In future the filter may be tested for various filter orders and with different desired signals generation.

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