

# Speed Control of Brushless DC Motor Implementing Extended Kalman Filter

Joyce Jacob, Surya Susan Alex, Asha Elizabeth Daniel

Abstract—BLDC motors or brushless dc motors are permanent magnet synchronous motors that work similar to dc motors. The rotor position information is important for the speed control of BLDC motor. Rotor position detection can be done using sensors which include the use of encoders or optical sensors. The Hall sensor are the most commonly used one. Also, sensor less techniques can be applied for the rotor position detection. The Extended Kalman Filter (EKF) is a sensor less method of rotor position detection wherein the rotor position is estimated from the machine parameters. In this paper, the BLDC motor has been modeled. Rotor position estimation using the Extended Kalman Filter (EKF) is done and speed control is achieved. Also, rotor position detection using Hall sensor signals is done and speed control is achieved. Here, the bipolar PWM technique with hard switching is employed.

*Index Terms*—BLDC motor, electronic commutation, Extended Kalman Filter, Hall sensor.

#### I. INTRODUCTION

The growing use of permanent magnets in electrical machines is due to the advantages such as no excitation losses, simplified construction, improved efficiency, fast dynamic performance, and high torque or power per unit volume. It was during the early 19<sup>th</sup> century that the permanent magnets were first used in electrical machines, but due to the poor quality of permanent magnet materials, it did not gain popularity until 1930. It was only after the 1930s that the better quality permanent magnet materials like Alnico were developed. Squirrel cage induction motors had gained popularity during the 20<sup>th</sup> century due to its rugged construction, but had the disadvantages of poor power factor and efficiency [1]. Synchronous motors and dc commutator motors on the other hand had to face the problems of speed, noise problems, wear and EMI due to the use of commutator and brushes. These led to the development of Permanent Magnet Brushless DC Motors (PMBLDC), simply referred to as Brushless DC (BLDC) motors. BLDC motors have gained popularity due to its better characteristics and performance. Also they are used in a great amount of industrial sectors because their architecture is suitable for any safety critical applications. From the modeling perspective, BLDC motors are dc motors inside out. While dc motors have a permanent magnet stator and rotor windings, the BLDC motors have a permanent magnet rotor and three phase distributed stator windings. They are characterized by a trapezoidal back emf. The commutation in dc motors is performed by commutators and brushes, while in BLDC motors, electronic commutation is employed. Speed control of BLDC motor requires the information regarding the rotor position. For speed control, the input voltage to the motor and hence the flux developed has to be controlled. For this, the BLDC motor is fed from a PWM controlled three phase inverter. The rotor position gives us information regarding the instant and duration for which any switch in the inverter has to be operated so that a particular commutation sequence is followed.

#### **II. METHODS OF ROTOR POSITION SENSING**

For the operation of the BLDC motor, it is important that the stator windings be energized in a proper sequence. For the correct switching of the inverter switches, the information regarding the rotor position is necessary. For this purpose, the rotor angular position needs to be detected using some method. There are two methods of rotor position detection. They are

- Sensor methods
- Sensor less methods

Using any of the above mentioned methods, the rotor position is detected and based on which the inverter switching is carried out so that the stator windings are energized in a particular sequence.

#### A. Sensor method

In sensor methods, an auxiliary device such as an optical encoder or resolver is used to detect the rotor position. Fig.1 shows the block diagram of a position sensor used for the rotor position detection [4]. Here the rotor position is used by a speed controller for motor speed control.



Fig.1. Block Diagram of Sensor Methods [4]

Different algorithms can be employed for the control of BLDC motors, like the Hysteresis control and pulse width modulation control (PWM) [8]. Hall Effect sensors are a common type of sensors used for the detection of rotor position sensors in BLDC motors.



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#### B. Sensor less method

The many disadvantages of the sensor methods have given way to the development of the sensor less methods. Sensor less methods offer many advantages [2].

- Low installation cost as the phase windings are • the only electrical connections to the machine.
- As there are no connecting leads to the controller, the position data will not be tampered by electromagnetic interference.
- Cost will be considerably less due to the elimination of the position encoding device.

There are many sensor less methods of rotor position detection, some of which are the Back emf Method, Rotor Position Detection from Third Harmonic of Back emf, Observer Based Method, Inductance Variation Sensing Method, Flux Linkage Variation Sensing, Parameter estimation using Extended Kalman Filter (EKF) etc.

#### **III. BLDC MOTOR MODEL**

The BLDC motor modeling is done based on its dynamic equations. For control of BLDC motor, we require information regarding it's rotor position. The rotor position information as well as the speed signal required for its speed control is obtained from the motor model. In the simulation work done here, the Hall sensor signals shown in table 1 are used. Corresponding to each rotor position detected, a Hall signal will be produced.

Equations used for BLDC motor modeling

Terms used [3]:		
e - Back emf.		
i – Line current.		
v- Terminal voltage.		
E- Back emf constant.		
N - no. of conductors co	nnected in series	per phase.
wm- Angular velocity		
Ø- Flux linkage		
R- Resistance of the state	or winding	
L – Inductance of the sta	tor winding	
M – mutual inductance		
J - moment of inertia		
<b>B-</b> Frictional coefficient		
T <sub>e</sub> – Motor developed to:	rque	
$T_1$ – load torque		
P- no. of poles		
The back emf is given by		
$e = E * f(\theta)$		(1)
where Back emf constant		
$E = N * \emptyset * w_m$		(2)
$f(\Theta) = 1$	0<	
$= (6/\pi)(\pi - \Theta) - 1$	$120 < \Theta < 180$	
= -1	$180 < \Theta < 300$	
$= (6/\pi)(\Theta - 2\pi) + 1$	300< ⊖ <360	(3)
The line current is obtained fi	rom the equation	
$\frac{di}{dt} = \frac{(v - R * i - e)}{(v - R * i - e)}$		
dt  (L+M)		(4)
The developed torque		

$$=\frac{(e_a i_a + e_b i_b + e_c i_c)}{(e_a i_a + e_b i_b + e_c i_c)}$$

(5)The motor speed is obtained from the equation  $J \frac{w_m}{dt} + Bw_m = (T_e - T_l)$ 

$$\frac{d\Theta}{dt} = \frac{P}{2} * w_m$$

(7)From the above dynamic equations, the BLDC motor modeling was done.

(6)

#### **IV. HALL SENSOR SIGNALS**

Hall effect sensors are a common type of sensors used for the detection of rotor position sensors in BLDC motors. Hall effect sensors comprise of three sensor unit's mounted on a permanent magnet disc. The sensors are placed 120 electrical degrees apart. The magnetic disc has two north poles and two south poles. Each time the north-south boundary crosses a sensor, the sensor output changes from a zero to a one or from a one to a zero. Depending upon the rotor position, the sensor gives a binary output comprising of a three bit word. With the three sensors, there is a possibility of eight digital codes, i.e., 000 to 111. Table 1 shows the Hall sensor signals corresponding to the rotor position.

	Hall sensor signals				
No.	Rotor position (degrees)	Hall signals	Phase energize d		
1	0-60	101	AB		
2	60-120	100	AC		
3	120-180	110	BC		
4	180-240	010	BA		
5	240-300	011	CA		
6	300-360	001	СВ		

Table	1.	Hall	sensor	signal	ls

Of these, only six digital codes are used, eliminating the use of the codes 000 and 111, which are considered as illegal values, to be flagged as fault conditions. The occurrence of the digital codes 000 and 111 as sensors outputs is an indication of bad connection, or some problem related to the hall sensor power supply. With the indication of the rotor position from the hall sensor output, we can determine the stator coils to be turned on and off to get the best torque response from the motor. So it is necessary to have an accurate detection of the rotor position.

### V. PARAMETER ESTIMATION USING EXTENDED **KALMAN FILTER (EKF)**

Extended Kalman Filter (EKF) is an effective state estimation algorithm that can be applied to non-linear systems. Regardless of the precision of the measurement variables, the EKF provides a quick and accurate estimate of the variables to be estimated [7]. In the context of BLDC



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Simulation results

Speed waveform

motors, EKF can be employed for estimating the speed and rotor position of the motor. The EKF algorithm has two steps [6] :

- Predictor step.
- Corrector step.

Predictor step

$$\hat{\mathbf{x}}_{(\mathbf{k}+1/\mathbf{k})} = \mathbf{F}_{\mathbf{k}} \hat{\mathbf{x}}_{(\mathbf{k}/\mathbf{k})} + \mathbf{G}_{\mathbf{k}} \mathbf{u}_{\mathbf{k}} \tag{8}$$

$$P_{(k+1/k)} = F'_{k} P_{(k/k)} F'^{1}_{k} + Q_{k}$$
(9)

Where F =I+AT,

G= BT T- sampling interval

$$F' = \frac{d(F_k x_{(k)} + G_k u_k)}{dx_k}$$
(10)

Corrector step

$$\mathbf{K}_{\mathbf{k}} = \widehat{\mathbf{P}}_{(\mathbf{k}+1/\mathbf{k})} \mathbf{H}^{\mathrm{T}} [\mathbf{H} \widehat{\mathbf{P}}_{(\mathbf{k}/\mathbf{k}+1)} \mathbf{H}^{\mathrm{T}} + \mathbf{R}_{\mathbf{k}}]^{\wedge} (-1).$$

$$\hat{\mathbf{R}}_{a} = [\mathbf{I} - \mathbf{K}_{a} \mathbf{H}]\hat{\mathbf{P}}_{a} \qquad (11)$$

$$\hat{\mathbf{x}}_{k/k} = \hat{\mathbf{x}}_{(k/k-1)} + \mathbf{K}_{k} [\mathbf{y}_{k} - \mathbf{H}\mathbf{x}_{(k/k-1)}]$$
(12)
(12)
(12)
(12)
(13)

P-Estimation error covariance.

Q- State noise covariance.

R- Measurement noise covariance.

Using the above equations, the rotor position and the motor speed can be estimated.

## VI. SIMULATION MODEL AND RESULTS

A. Speed control of BLDC motor using Hall sensor signals

Simulation Model



Fig.2 simulation model with Hall Sensor signals



#### Fig. 3 Speed waveform

For a reference speed of 300rpm, the motor speed waveforms are obtained, and they are found to be close to the reference speed value.

Back emf waveform



Fig.4 Waveforms for Back emf

The trapezoidal back emf waveforms are obtained. The emf waveforms obtained are phase shifted by 120 degrees. *Current waveform* 



**Fig.5 waveforms for current** The line current waveforms were obtained.



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Fig.6 waveforms for terminal voltage The terminal voltage waveforms were obtained. *Torque Waveform* 



**Fig.7 waveforms for torque developed** The load torque value used for simulation is 2Nm. The developed torque has an average value of around 2Nm.

# B. Speed control of BLDC motor using Extended Kalman Filter Algorithm

Simulation model



Fig.8 Simulation model with EKF Simulation results Speed waveform



With Extended Kalman Filter the estimated motor speed was found close to the actual speed.

### VII. CONCLUSION

The Permanent Magnet Brushless DC Motor (PMBLDC) are gaining popularity because of it's performance and reliability. Sensor based speed control techniques have widespread application but they have certain disadvantages like cost, size etc. So, nowadays the present focus is on sensor less techniques like the EKF. Advancement in power electronics and DSP based technologies present possibilities of improved control of BLDC motors. Also Application Specific Integrated Circuits (ASIC) offer low cost control of BLDC motors. In this paper, modeling of BLDC motor for speed control is done. The rotor position information is obtained using both, the Hall sensor signals and the Extended Kalman Filter Algorithm. The simulation results show that the speed control results obtained using the Extended Kalman Filter Algorithm is comparable to that obtained using the Hall sensor signals.

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